

# INTERNATIONAL GCSE

## Further Pure Mathematics (9-1)

### SAMPLE ASSESSMENT MATERIALS

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Pearson Edexcel International GCSE in Further Pure Mathematics (4PM1)

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For first teaching September 2017

First examination June 2019



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# Introduction

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The Pearson Edexcel International GCSE in Further Pure Mathematics is designed for use in schools and colleges. It is part of a suite of International GCSE qualifications offered by Pearson.

These sample assessment materials have been developed to support this qualification and will be used as the benchmark to develop the assessment students will take.



## General marking guidance

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These notes offer general guidance, but the specific notes for examiners appertaining to individual questions take precedence.

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## Guidance on the use of abbreviations

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<b>M</b>	method mark awarded for a correct method or partial method
<b>B</b>	unconditional accuracy mark (no method needed)
<b>A</b>	accuracy mark (awarded after a correct method or process; if no method or process is seen then full marks for the question are implied but see individual mark schemes for more details)
<b>oe</b>	or equivalent
<b>cao</b>	correct answer only
<b>ft</b>	follow through (when appropriate as per mark scheme)
<b>sc</b>	special case
<b>dep</b>	dependent (on a previous mark)
<b>indep</b>	independent
<b>awrt</b>	answer which rounds to
<b>isw</b>	ignore subsequent working
<b>ee</b>	each error
<b>oo</b>	or omission
<b>cc</b>	correct conclusion
<b>ncc</b>	not corrected correctly
<b>dp</b>	decimal place



Write your name here

Surname	Other names
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# Further Pure Mathematics

## Level 2

## Paper 1



Sample assessment material for first teaching September 2017 <b>Time: 2 hours</b>	Paper Reference <b>4PM1/01</b>
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**Calculators may be used.**

Total Marks

### Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.  
Anything you write on the formulae page will gain NO credit.

### Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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# International GCSE in Further Pure Mathematics Formulae sheet

## Mensuration

Surface area of sphere =  $4\pi r^2$

Curved surface area of cone =  $\pi r \times$  slant height

Volume of sphere =  $\frac{4}{3}\pi r^3$

## Series

### Arithmetic series

Sum to  $n$  terms,  $S_n = \frac{n}{2}[2a + (n-1)d]$

### Geometric series

Sum to  $n$  terms,  $S_n = \frac{a(1-r^n)}{(1-r)}$

Sum to infinity,  $S_\infty = \frac{a}{1-r} \quad |r| < 1$

### Binomial series

$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$

## Calculus

### Quotient rule (differentiation)

$$\frac{d}{dx} \left( \frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

## Trigonometry

### Cosine rule

In triangle  $ABC$ :  $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

## Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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**Answer all ELEVEN questions.**

**Write your answers in the spaces provided.**

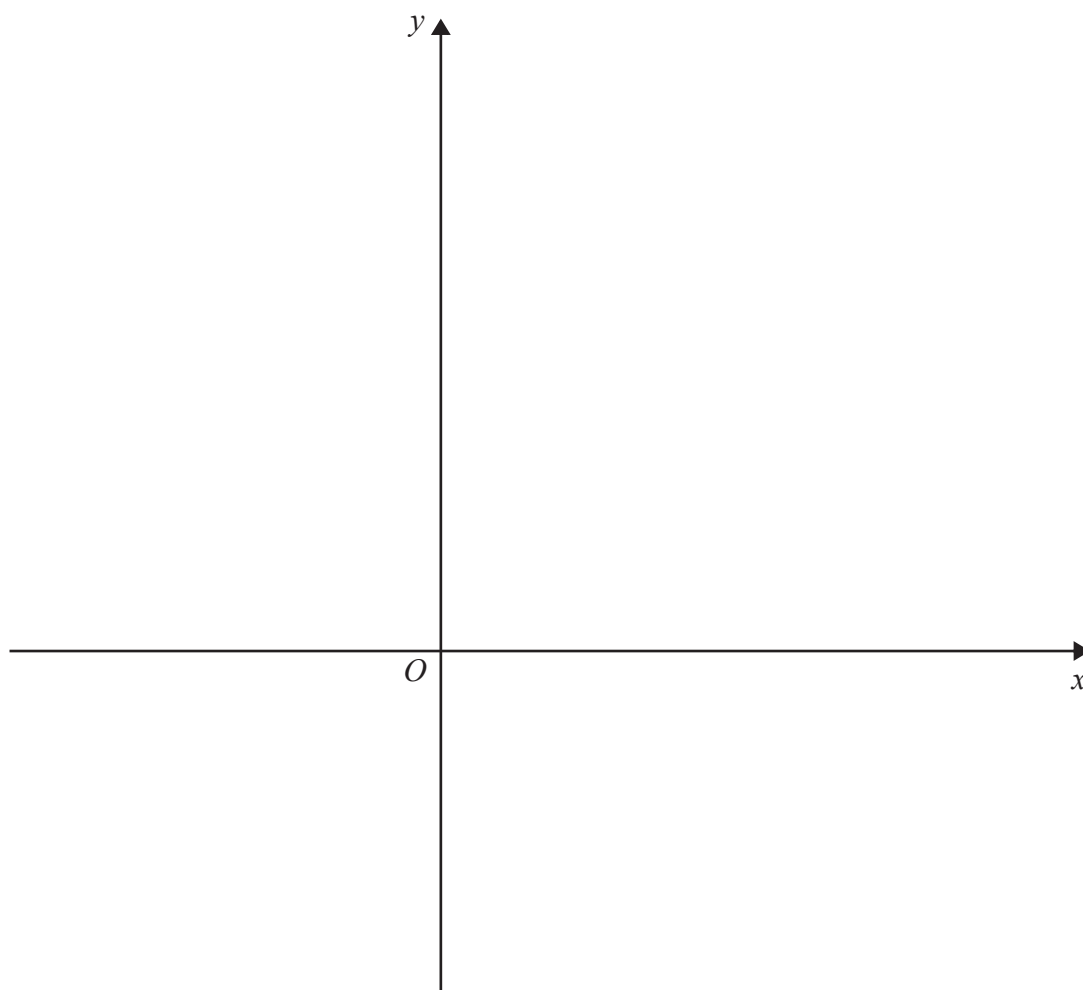
**You must write down all the stages in your working.**

- 1** (a) On the axes below, sketch the lines with equations  $2x + 3y = 8$  and  $2y = 4x + 1$

On your sketch, show the coordinates of the points where the lines cross the coordinate axes. (2)

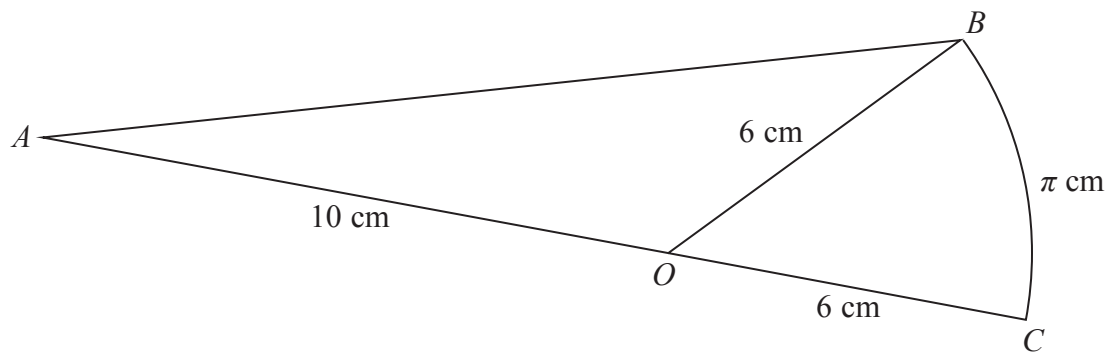
- (b) Show, by shading on your sketch, the region  $R$  defined by the inequalities

$$2x + 3y \leq 8 \quad 2y \leq 4x + 1 \quad y \geq 0 \quad x \leq 2 \quad (2)$$



**(Total for Question 1 is 4 marks)**

Diagram NOT  
accurately drawn



**Figure 1**

Figure 1 shows a shape  $ABC$  in which  $AOB$  is a triangle,  $AOC$  is a straight line and  $OBC$  is a sector of a circle with centre  $O$ .

$AO = 10$  cm,  $OC = OB = 6$  cm and the length of arc  $BC = \pi$  cm.

Find, to 3 significant figures,

(a) the length of  $AB$ , (3)

(b) the area of the shape  $ABC$ . (3)

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**Question 2 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 2 is 6 marks)**

3 Solve, in degrees to 1 decimal place, for  $0 \leq \theta < 180$

$$2 \cos(2\theta + 30)^\circ + \tan(2\theta + 30)^\circ = 0$$

(6)

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**Question 3 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 3 is 6 marks)**

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- 4 A particle  $P$  is moving along the  $x$ -axis.

At time  $t$  seconds ( $t \geq 0$ ) the velocity,  $v$  m/s, of  $P$  is given by  $v = 4t^2 - 19t + 12$

- (a) Find the values of  $t$  for which  $P$  is instantaneously at rest.

(2)

When  $t = 0$ , the displacement of  $P$  from the origin is  $-4$  m.

- (b) Find the displacement of  $P$  from the origin when  $t = 6$

(4)

At time  $t$  seconds the acceleration of  $P$  is  $a \text{ m/s}^2$ .

- (c) Find the value of  $t$  when  $a = 0$

(3)



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**Question 4 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 4 is 9 marks)**

- 5** Two numbers  $x$  and  $y$  are such that  $2x + y = 13$

The sum of the squares of  $2x$  and  $y$  is  $S$ .

- (a) Show that  $S = 8x^2 - 52x + 169$

(3)

Using calculus,

- (b) find the value of  $x$  for which  $S$  is a minimum, justifying that this value of  $x$  gives a minimum value for  $S$ .

(4)

- (c) find the minimum value of  $S$ .

(2)

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**Question 5 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 5 is 9 marks)**

6

$$y = e^x(x^2 - 3x)$$

Show that  $y - 2\frac{dy}{dx} + \frac{d^2y}{dx^2} = 2e^x$

(8)

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- 7 (a) Complete the table of values for

$$y = 2^{\left(\frac{x}{2}+1\right)} + 1$$

giving your answers to 2 decimal places where appropriate.

(2)

$x$	0	1	2	3	4	5
$y$	3				9	12.31

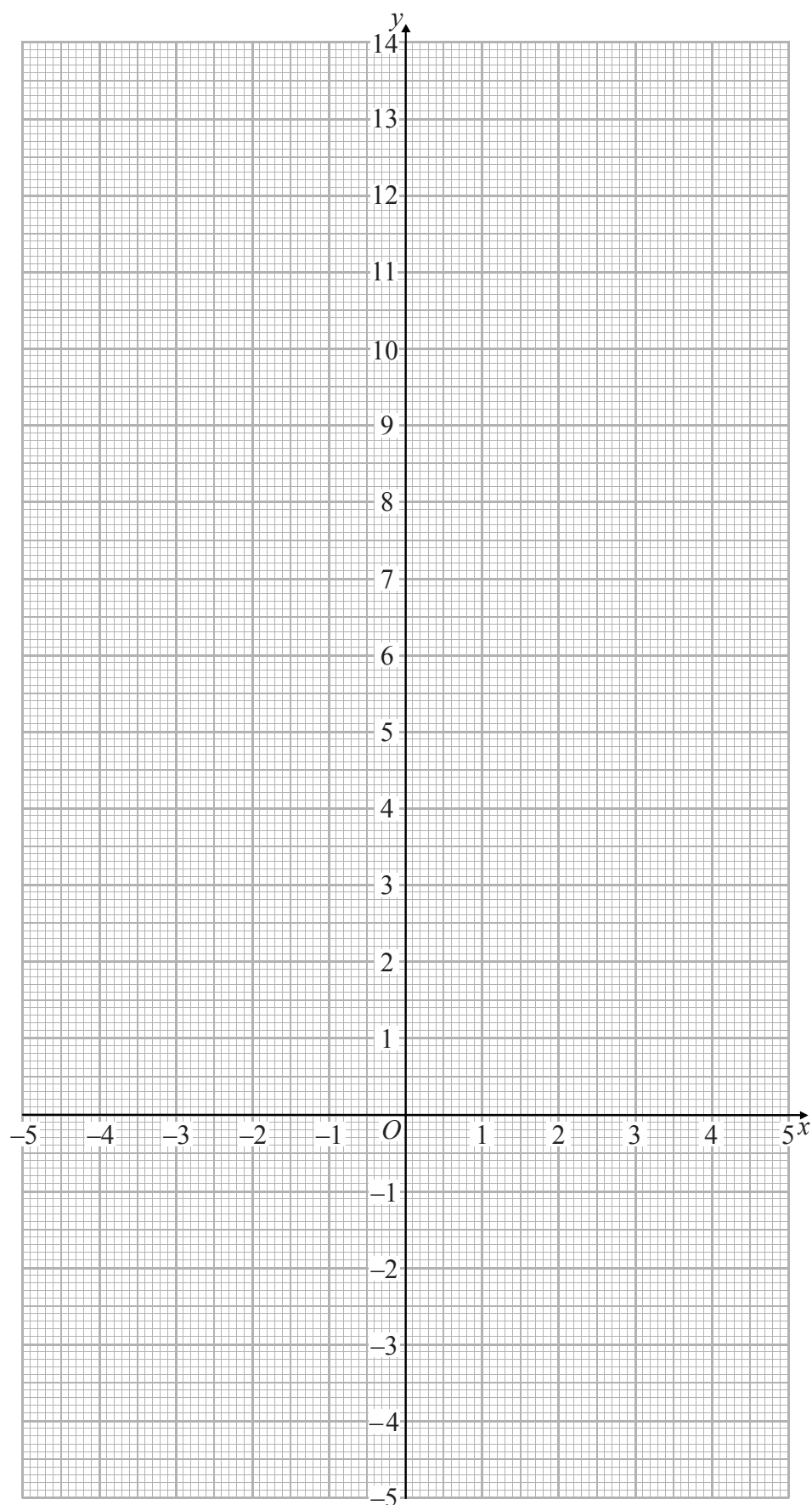
- (b) On the grid opposite, draw the graph of  $y = 2^{\left(\frac{x}{2}+1\right)} + 1$  for  $0 \leq x \leq 5$

(2)

- (c) By drawing a suitable straight line on the grid, obtain an estimate, to 1 decimal place, of the root of the equation  $\log_2(4x - 6)^2 - x = 2$  in the interval  $0 \leq x \leq 5$

(4)

Question 7 continued



(Total for Question 7 is 8 marks)

8 The sum  $S_n$  of the first  $n$  terms of an arithmetic series is given by  $S_n = 2n(n + 3)$

(a) Find the first term of the series.

(1)

(b) Find the common difference of the series.

(2)

The  $n$ th term of the series is  $T_n$

Given that  $6S_{(n-4)} = 7T_{(n+3)}$

(c) find the value of  $n$ .

(6)



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**Question 8 continued**

*(This area contains horizontal dotted lines for writing answers.)*

**(Total for Question 8 is 9 marks)**

- 9 The roots of a quadratic equation are  $\alpha$  and  $\beta$  where  $\alpha + \beta = -\frac{7}{3}$  and  $\alpha\beta = -2$
- (a) Find a quadratic equation, with integer coefficients, which has roots  $\alpha$  and  $\beta$

(4)

Given that  $\alpha > \beta$  and without solving the equation,

- (b) show that  $\alpha - \beta = \frac{11}{3}$

(2)

- (c) form a quadratic equation, with integer coefficients, which has roots

$$\frac{\alpha + \beta}{\alpha} \text{ and } \frac{\alpha - \beta}{\beta}$$

(7)

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Question 9 continued

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(Total for Question 9 is 13 marks)

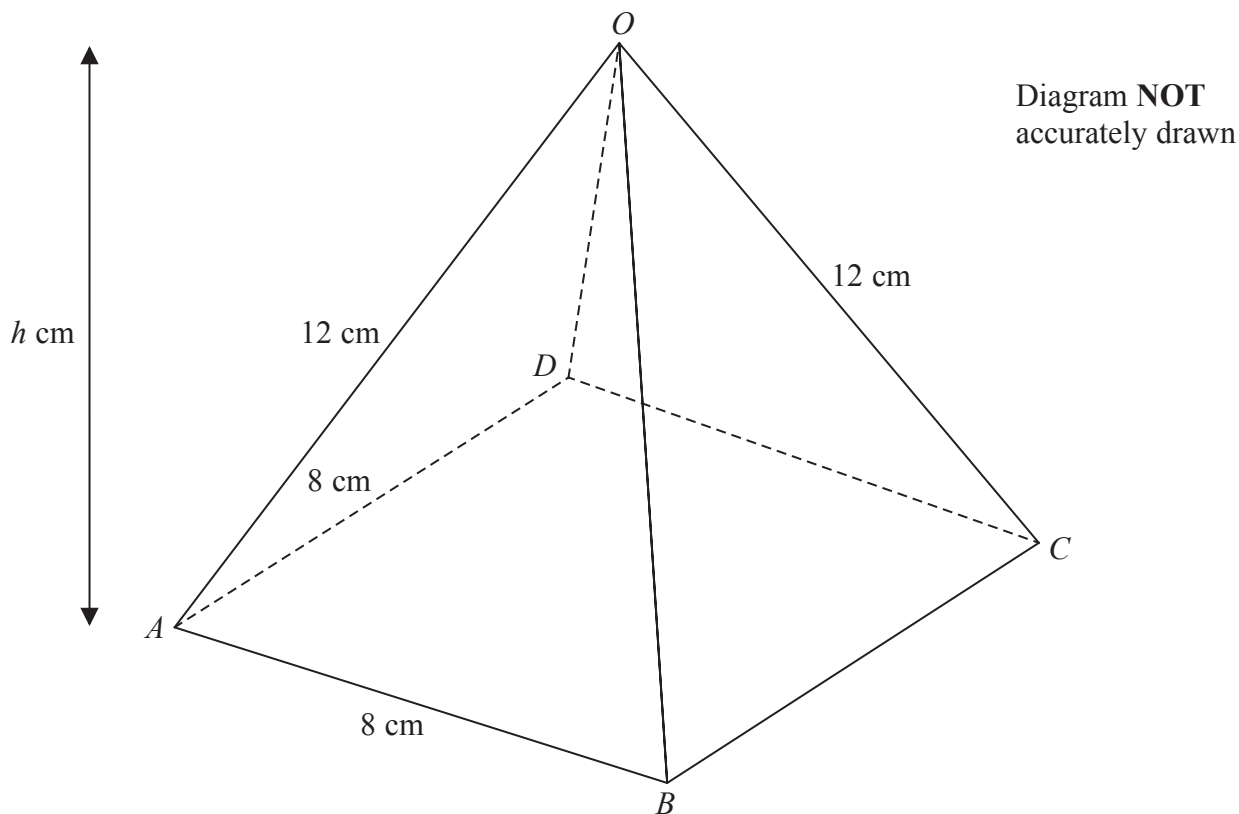


Figure 2

Figure 2 shows a right pyramid  $ABCD O$  with a horizontal square base of side 8 cm. The vertical height of the pyramid is  $h$  cm and  $OA = OB = OC = OD = 12$  cm.

- (a) Find the exact value of  $h$ . (3)
- (b) Find, to 1 decimal place, the size of the angle between  $OA$  and the plane  $ABCD$ . (2)
- (c) Find, to 1 decimal place, the size of the angle between the plane  $AOB$  and the plane  $ABCD$ . (2)

The midpoint of  $OA$  is  $P$  and  $Q$  is the point on  $BC$  such that  $BQ : QC = 3 : 1$

- (d) Show that  $PQ = 4\sqrt{5}$  cm. (4)
- (e) Find, to 1 decimal place, the size of angle  $PQA$ . (4)

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Question 10 continued

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**Question 10 continued**

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**Question 10 continued**

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**(Total for Question 10 = 15 marks)**

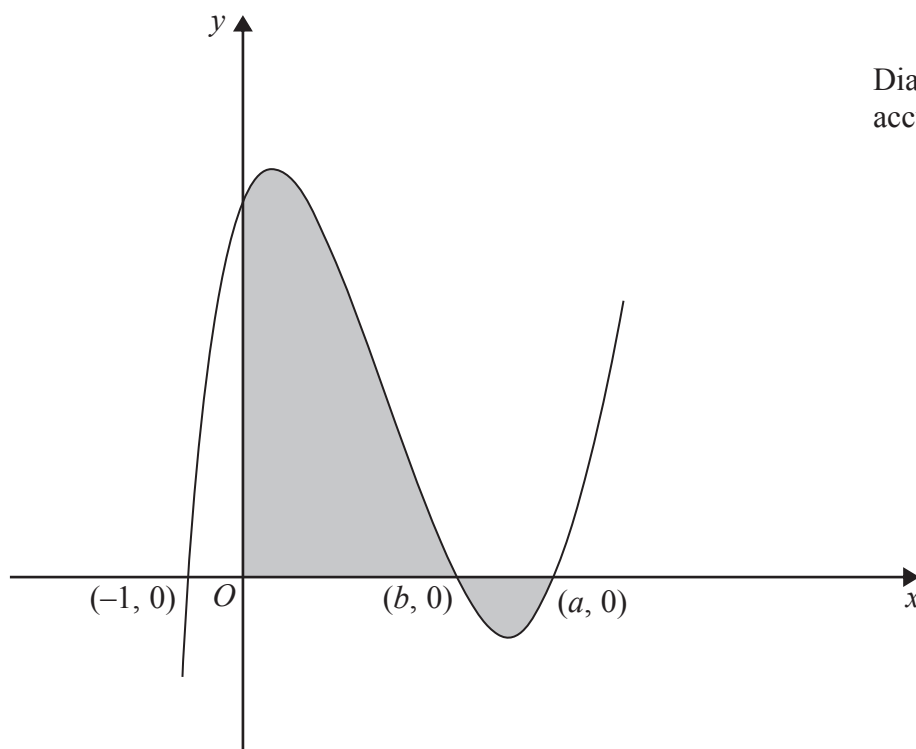


Diagram **NOT**  
accurately drawn

**Figure 3**

Figure 3 shows a sketch of the curve with equation  $y = f(x)$ , which passes through the points with coordinates  $(-1, 0)$ ,  $(b, 0)$  and  $(a, 0)$  where  $0 < b < a$ .

Given that  $f'(x) = 6x^2 - 26x + 12$

(a) find,

(i) the value of  $a$ ,

(ii) the value of  $b$ .

(8)

(b) Use algebraic integration to determine the exact value of the total area of the shaded regions shown in Figure 3.

(5)

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**Question 11 continued**

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**Question 11 continued**

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(Total for Question 11 is 15 marks)

**TOTAL FOR PAPER IS 100 MARKS**

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International GCSE Further Pure Mathematics – Paper 1 mark scheme

Paper 1				
Question	Working	Answer	Mark	AO
1 (a)				
(b)				
			B1 B1	1
			B1 B1	1
			(4)	
				One correct line Both correct lines Correct line $x = 2$ drawn Correct region shaded in or out.

Question	Working	Answer	Mark	AO	Notes
2 (a)	$\pi = 6\theta \Rightarrow \theta = \frac{\pi}{6} \Rightarrow \angle AOB = \frac{5\pi}{6} = (150^\circ)$ $AB = \sqrt{10^2 + 6^2 - 2 \times 10 \times 6 \times \cos\left(\frac{5\pi}{6}\right)} = 15.4894... = 15.5 \text{ cm}$	15.5 (cm)	B1	1	Accept working in degrees
(b)	$\text{Area} = \frac{1}{2} \times 10 \times 6 \times \sin \frac{5\pi}{6} + \frac{\pi}{6} \times \frac{6^2}{2} = 24.424...$	24.4 (cm <sup>2</sup> )	M1M1A1	2	$\angle AOB = 150^\circ$
	<b>ALTERNATIVE</b> $\text{Area} = \frac{1}{2} \times 10 \times 6 \times \sin \frac{5\pi}{6} + \frac{1}{2} \times \pi \times 6 = 24.424...$		M1M1A1 (6)		
3	$2 \cos(2\theta + 30) + \frac{\sin(2\theta + 30)}{\cos(2\theta + 30)} = 0 \Rightarrow 2 \cos^2(2\theta + 30) + \sin(2\theta + 30) = 0$ $\Rightarrow 2 - 2 \sin^2(2\theta + 30) + \sin(2\theta + 30) = 0$ $\sin(2\theta + 30) = \frac{1 \pm \sqrt{1 - 4 \times 2 \times (-2)}}{2 \times 2} = 1.2807..., -0.7807...$ $2\theta + 30 = -51.33167..., 231.33167, 308.66833$ $\theta = 100.7, 139.3$	$\theta = 100.7, 139.3$	M1 M1A1 M1 A1A1 (6)	2  3	Solves 3 TQ Finds one angle from their 3TQ

Question	Working	Answer	Mark	AO	Notes
<b>4</b>					
(a)	$v = 0$ so $4t^2 - 19t + 12 = 0 \Rightarrow (4t - 3)(t - 4) = 0 \Rightarrow t = \frac{3}{4}, 4$	$t = \frac{3}{4}, 4$	M1A1	1	
(b)	$s = \int 4t^2 - 19t + 2 dt = \frac{4t^3}{3} - \frac{19t^2}{2} + 12t + c$ when $t = 0, s = -4 \Rightarrow c = -4$ When $t = 6, s = \frac{4 \times 6^3}{3} - \frac{19 \times 6^2}{2} + 12 \times 6 - 4 = 14$	14	M1M1A1	2	
(c)	$a = \frac{dv}{dt} = 8t - 19 \Rightarrow 8t - 19 = 0 \Rightarrow t = \frac{19}{8}$	$t = \frac{19}{8}$	A1 M1M1A1 (9)	3	
<b>5</b>					
(a)	$2x + y = 13 \Rightarrow y = 13 - 2x$ $S = 4x^2 + (13 - 2x)^2 = 4x^2 + 169 - 52x + 4x^2 = 8x^2 - 52x + 169$	$8x^2 - 52x + 169$	B1	1	
(b)	$\frac{dS}{dx} = 16x - 52, \frac{dS}{dx} = 0 \Rightarrow 16x - 52 = 0 \Rightarrow x = \frac{13}{4}$ $\frac{d^2S}{dx^2} = 16, 16 > 0,$	$x = \frac{13}{4}$ Hence minimum	M1A1 M1M1A1 B1	2,3	
(c)	$S = 8 \times \left(\frac{13}{4}\right)^2 - 52 \times \frac{13}{4} + 169 = \frac{169}{2} = 84.5$	$\frac{169}{2} = 84.5$	M1A1 (9)	3	

Question	Working	Answer	Mark	AO	Notes														
6	$\frac{dy}{dx} = e^x(x^2 - 3x) + e^x(2x - 3) \Rightarrow e^x(2x - 3) = \frac{dy}{dx} - y$ $\frac{d^2y}{dx^2} = e^x(x^2 - 3x) + e^x(2x - 3) + e^x(2x - 3) + 2e^x = y + 2\left(\frac{dy}{dx} - y\right) + 2e^x$ $2e^x = \frac{d^2y}{dx^2} - 2\left(\frac{dy}{dx} - y\right) - y \Rightarrow 2e^x = y - 2\frac{dy}{dx} + \frac{d^2y}{dx^2} *$		M1M1A1  M1A1  M1M1A1 (8)	4  4															
7	<table border="1"><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>y</td><td>3</td><td>3.83</td><td>5</td><td>6.66</td><td>9</td><td>12.31</td></tr></table> <p>All points plotted within an accuracy of half of a square. A smooth curve drawn through their points</p>	x	0	1	2	3	4	5	y	3	3.83	5	6.66	9	12.31			1	
x	0	1	2	3	4	5													
y	3	3.83	5	6.66	9	12.31													
(a)			B1B1																
(b)			B1B1																
(c)	$\log_2(4x - 6)^2 - x = 2 \Rightarrow 2\log_2(4x - 6) = x + 2 \Rightarrow \log_2(4x - 6) = \frac{x}{2} + 1$ $\Rightarrow 4x - 6 = 2^{\left(\frac{x}{2} + 1\right)} \Rightarrow 4x - 5 = 2^{\left(\frac{x}{2} + 1\right)} + 1$ <p>Line <math>y = 4x - 5</math> drawn on graph <math>\Rightarrow</math> so <math>x = 2.8(36)</math></p>	$x = 2.8$	M1M1  M1A1 (8)	2															





Question	Working	Answer	Mark	AO	Notes
9 (a)	$\alpha + \beta = -\frac{7}{3}$ $\alpha\beta = -2 = -\frac{6}{3}$ so $a = 3$ , $b = 7$ and $c = -6$ Hence quadratic equation $\Rightarrow 3x^2 + 7x - 6 = 0$ oe with integer coefficients		B1B1 M1A1	1	
(b)	$(\alpha - \beta)^2 = \alpha^2 + \beta^2 - 2\alpha\beta = (\alpha + \beta)^2 - 4\alpha\beta = \left(-\frac{7}{3}\right)^2 - 4 \times -2 = \frac{121}{9}$ $\alpha > \beta$ so $\alpha - \beta = \frac{11}{3}$ *		M1A1	3	
(c)	Sum $\frac{\alpha + \beta}{\alpha} + \frac{\alpha - \beta}{\beta} = \frac{\beta(\alpha + \beta) + \alpha(\alpha - \beta)}{\alpha\beta} = \frac{\alpha^2 + \beta^2}{\alpha\beta} = \frac{\left(-\frac{7}{3}\right)^2 - 2 \times -2}{-2} = -\frac{85}{18}$ Product $\frac{(\alpha + \beta)}{\alpha} \times \frac{(\alpha - \beta)}{\beta} = \frac{\left(-\frac{7}{3}\right) \times \left(\frac{11}{3}\right)}{-2} = \frac{77}{18}$ Equation $18y^2 + 85y + 77 = 0$ oe with integer coefficients		M1M1A1  M1A1 M1A1 (13)	3	

Question	Working	Answer	Mark	AO	Notes
<b>10</b>	Let $M$ be the midpoint of diagonals $AC$ or $DB$				
(a)	$AC = \sqrt{8^2 + 8^2} = 8\sqrt{2} \Rightarrow AM = 4\sqrt{2}$ $h = \sqrt{12^2 - (4\sqrt{2})^2} = \sqrt{112} = (4\sqrt{7})$	$4\sqrt{7}$	M1M1A1	1	
(b)	$\tan^{-1}\left(\frac{4\sqrt{7}}{4\sqrt{2}}\right) = 61.87449... \approx 61.9^\circ$	$61.9^\circ$	M1A1	1	Or any equivalent trigonometry
(c)	Let $N$ be the midpoint of $AB$				
	Angle the plane $AOB$ makes with horiz = $\tan^{-1}\left(\frac{4\sqrt{7}}{4}\right) = 69.295... \approx 69.3^\circ$	$69.3^\circ$	M1A1	3	Or any equivalent trigonometry
(d)	<p><b>By using the symmetrical properties of the pyramid</b></p> <p>Let <math>S</math> be the perpendicular from <math>P</math> to diagonal <math>AC</math>  Let <math>R</math> be the perpendicular from <math>S</math> to side <math>BC</math></p> <p>In triangle <math>PSR \quad \rightarrow \quad PR = \sqrt{(2\sqrt{17})^2 - 2^2} = 8</math>  In triangle <math>PRQ \quad \rightarrow \quad PQ = \sqrt{8^2 + 4^2} = 4\sqrt{5}</math></p>	$4\sqrt{5}$	M1A1 M1A1	3	Or any equivalent system of right angle triangles
(e)	<p>Length <math>AQ = \sqrt{8^2 + 6^2} = 10</math></p> <p>Angle of <math>PQA = \cos^{-1}\left(\frac{10^2 + (4\sqrt{5})^2 - 6^2}{2 \times 10 \times 4\sqrt{5}}\right) = 36.39124... \approx 36.4^\circ</math></p>	$36.4^\circ$	M1 M1A1A1 (15)	3	

Question	Working	Answer	Mark	AO	Notes
(d)	<p><b>ALTERNATIVE without using the symmetrical properties of the pyramid</b></p> $\cos OAB = \frac{12^2 + 8^2 - 12^2}{2 \times 8 \times 12} = \frac{1}{3}$ $\Rightarrow PB = \sqrt{6^2 + 8^2 - 2 \times 6 \times 8 \times \frac{1}{3}} = 2\sqrt{17}$ <p>In triangle <math>PBC</math></p> $PC = \sqrt{6^2 + (8\sqrt{2})^2 - 2 \times 6 \times (8\sqrt{2}) \times \cos\left(\tan^{-1}\left(\frac{\sqrt{7}}{\sqrt{2}}\right)\right)} = 10$ $\Rightarrow \text{Angle } PBC = \cos^{-1}\left(\frac{8^2 + 68 - 10^2}{2 \times 8 \times 2\sqrt{17}}\right) = 75.9637\dots^\circ$ <p>In triangle <math>PBQ</math>;</p> $PQ = \sqrt{6^2 + 68 - 2 \times 6 \times 2\sqrt{17} \times \cos 75.96375\dots} = 4\sqrt{5}$	$4\sqrt{5}$	M1          M1A1	3	

Question	Working	Answer	Mark	AO	Notes
<b>11</b>	Mark parts (i) and (ii) together			1, 3	
<b>(a)</b>	$y = \int 6x^2 - 26x + 12 \, dx = \left[ \frac{6x^3}{3} - \frac{26x^2}{2} + 12x + c \right]$ <p>At the point <math>(-1, 0)</math></p> $0 = 2(-1)^3 - 13(-1)^2 + 12(-1) + C \Rightarrow C = 27$	M1			
			M1A1		
	$(2x^3 - 13x^2 + 12x + 27) \div (x + 1) = 2x^2 - 15x + 27 = (2x - 9)(x - 3)$ $\Rightarrow a = \frac{9}{2}, b = 3$	$a = \frac{9}{2}, b = 3$	M1M1A1 B1B1		
<b>(b)</b>	$\text{Area} = \int_0^3 2x^3 - 13x^2 + 12x + 27 \, dx + \left  \int_3^9 2x^3 - 13x^2 + 12x + 27 \, dx \right  =$ $\left[ \frac{2}{4}x^4 - \frac{13}{3}x^3 + \frac{12}{2}x^2 + 27x \right]_0^3 + \left[ \frac{2}{4}x^4 - \frac{13}{3}x^3 + \frac{12}{2}x^2 + 27x \right]_3^9 = \frac{2043}{32}$ <p>So Area = <math>\frac{2043}{32}</math></p>	$\frac{2043}{32}$	M1M1 A1M1A1	3	
		Area = $\frac{2043}{32}$	(13)		
		<b>Total</b>	<b>100</b>		



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Surname

Other names

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International GCSE**

Centre Number

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Candidate Number

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# Further Pure Mathematics

**Level 2  
Paper 2**



Sample assessment material for first teaching September 2017

**Time: 2 hours**

Paper Reference

**4PM1/02**

**Calculators may be used.**

Total Marks

## Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.  
Anything you write on the formulae page will gain NO credit.

## Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

## Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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**PEARSON**

# International GCSE in Further Pure Mathematics Formulae sheet

## Mensuration

Surface area of sphere =  $4\pi r^2$

Curved surface area of cone =  $\pi r \times$  slant height

Volume of sphere =  $\frac{4}{3}\pi r^3$

## Series

### Arithmetic series

Sum to  $n$  terms,  $S_n = \frac{n}{2}[2a + (n-1)d]$

### Geometric series

Sum to  $n$  terms,  $S_n = \frac{a(1-r^n)}{(1-r)}$

Sum to infinity,  $S_\infty = \frac{a}{1-r}$   $|r| < 1$

### Binomial series

$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots$  for  $|x| < 1, n \in \mathbb{Q}$

## Calculus

### Quotient rule (differentiation)

$$\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

## Trigonometry

### Cosine rule

In triangle  $ABC$ :  $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

## Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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**Answer all ELEVEN questions.**

**Write your answers in the spaces provided.**

**You must write down all the stages in your working.**

- 1** The  $n$ th term of a geometric series is  $3e^{(1-2n)}$

Find the sum to infinity of this series.

Give your answer in the form  $\frac{ae}{e^b - 1}$  where  $a$  and  $b$  are integers to be found.

**(5)**

**(Total for Question 1 is 5 marks)**

2 Find the set of values of  $x$  for which

(a)  $3 + x < 2x - 1$

(1)

(b)  $x(x - 1) > 6$

(3)

(c) **both**  $3 + x < 2x - 1$  **and**  $x(x - 1) > 6$

(1)

(Total for Question 2 is 5 marks)

3  $O$ ,  $A$  and  $B$  are fixed points such that

$$\overrightarrow{OA} = 4\mathbf{i} + 3\mathbf{j} \quad \overrightarrow{OB} = 8\mathbf{i} + p\mathbf{j} \quad \text{and} \quad |\overrightarrow{AB}| = 2\sqrt{13}$$

(a) Find the possible values of  $p$ .

(3)

Given that  $p > 0$

(b) find a unit vector parallel to  $\overrightarrow{AB}$

(2)

(Total for Question 3 is 5 marks)



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**Question 4 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 4 is 10 marks)**

5 (a) Show that  $\cos(A - B) - \cos(A + B) = 2 \sin A \sin B$  (2)

(b) Hence express  $2 \sin 5x \sin 3x$  in the form  $\cos mx - \cos nx$  where  $m$  and  $n$  are integers, giving the value of  $m$  and the value of  $n$ , (1)

(c) (i) Find  $\int 4 \sin 5\theta \sin 3\theta \, d\theta$

(ii) Hence evaluate  $\int_0^{\frac{\pi}{6}} 4 \sin 5\theta \sin 3\theta \, d\theta$ , giving your answer in the form  $\frac{a\sqrt{b}}{c}$  where  $a$ ,  $b$  and  $c$  are integers. (4)

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**Question 5 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 5 is 7 marks)**

6 Solve the equation  $\log_2 x + 6\log_x 2 = 7$

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**Question 6 continued**

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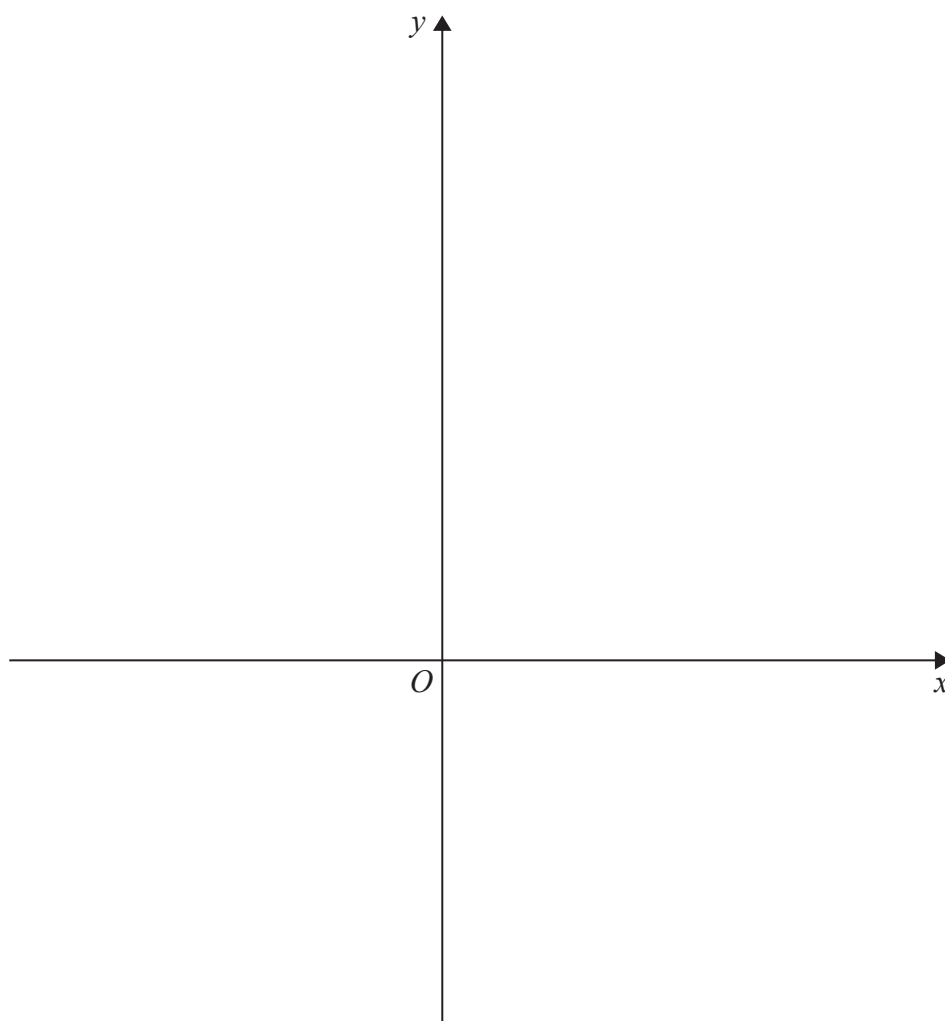
**(Total for Question 6 is 7 marks)**

7 The curve  $C$  with equation

$$y = \frac{ax - 5}{x - b}$$

where  $a$  and  $b$  are integers, crosses the  $x$ -axis at the point  $(2.5, 0)$ . The asymptote to  $C$  which is parallel to the  $y$ -axis has equation  $x = 1$

- (a) (i) Show that  $a = 2$  (3)
- (ii) Find the value of  $b$ . (1)
- (b) Find the coordinates of the point where  $C$  crosses the  $y$ -axis. (1)
- (c) Find the equation of the asymptote to  $C$  which is parallel to the  $x$ -axis. (1)
- (d) Using the axes below, sketch the curve  $C$  showing clearly the asymptotes and the coordinates of the points where  $C$  crosses the coordinate axes. (3)



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**Question 7 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 7 is 8 marks)**

- 8 (a) Expand  $\frac{3}{\sqrt{1-2x}}$  in ascending powers of  $x$  up to and including the term in  $x^3$  and simplifying each term as far as possible. (4)
- (b) Write down the range of values of  $x$  for which this expansion is valid. (1)
- (c) Show that  $\frac{3}{\sqrt{0.9}} = \sqrt{10}$  (1)
- (d) Express  $\frac{1}{\sqrt{10}-3}$  in the form  $a\sqrt{10} + b$ , where  $a$  and  $b$  are integers. (2)
- (e) Hence, using your expansion with a suitable value for  $x$ , obtain an approximation to 5 decimal places of  $\frac{1}{\sqrt{10}-3}$  (3)

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**Question 8 continued**

Handwriting practice area with horizontal dotted lines.

**(Total for Question 8 is 11 marks)**

9

$$f(x) = 7 + 4x - 2x^2$$

Given that  $f(x)$  can be written in the form  $P(x + Q)^2 + R$  where  $P$ ,  $Q$  and  $R$  are constants,

(a) find the value of  $P$ , the value of  $Q$  and the value of  $R$ . (3)

(b) hence write down

- (i) the maximum value of  $f(x)$ ,  
(ii) the value of  $x$  for which this maximum occurs. (2)

The curve  $C$  has equation  $y = 7 + 4x - 2x^2$

The line  $l$  with equation  $y = 4 - x$  intersects  $C$  at two points.

(c) Find the  $x$  coordinates of these two points. (3)

The finite region bounded by the curve  $C$  and the line  $l$  is rotated  $360^\circ$  about the  $x$ -axis.

(d) Use algebraic integration to find, to 3 significant figures, the volume of the solid generated. (5)

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Question 9 continued

Handwriting practice area with horizontal dotted lines.

**Question 9 continued**

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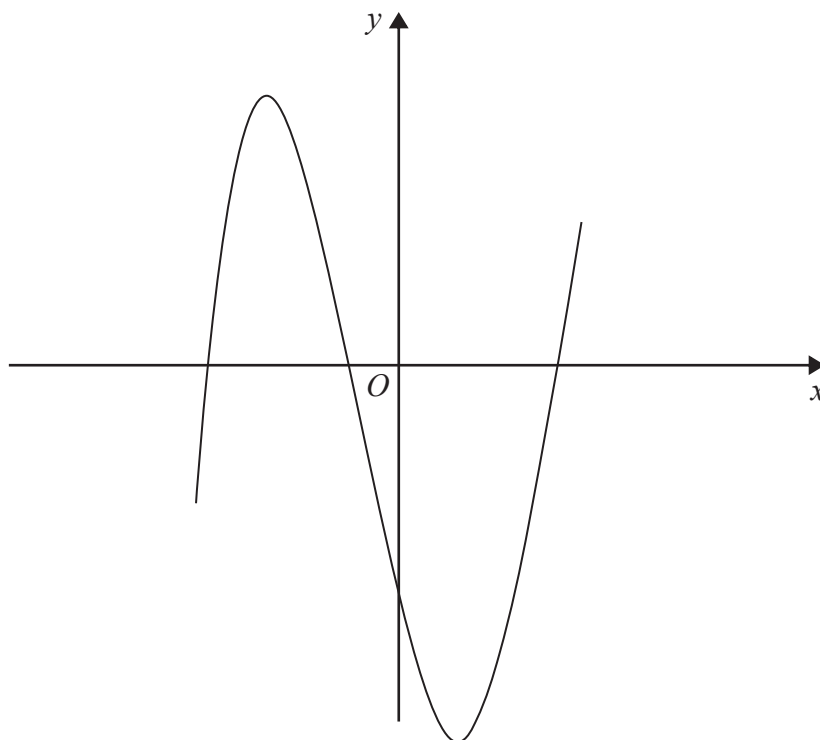
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**Question 9 continued**

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**(Total for Question 9 is 13 marks)**



**Figure 1**

Figure 1 shows the curve  $M$  with equation  $y = x^3 - 13x - 12$

The point  $P$ , with  $x$  coordinate  $-2$ , lies on  $M$  and line  $l_1$  is the tangent to  $M$  at the point  $P$ .

- (a) Find an equation for  $l_1$  (5)

The point  $Q$  lies on  $M$  and the line  $l_2$  is the tangent to  $M$  at the point  $Q$ .

Given that  $l_1$  and  $l_2$  are parallel,

- (b) find an equation for  $l_2$  (4)

The normal to  $M$  at  $P$  meets  $l_2$  at the point  $R$ .

- (c) Find the coordinates of  $R$ . (4)

- (d) Find the exact length of the line  $PR$ . (2)

The tangent and normal at  $P$  and the tangent and normal at  $Q$  form a rectangle.

- (e) Find the exact area of this rectangle. (3)

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**Question 10 continued**

Handwriting practice area with horizontal dotted lines.

**Question 10 continued**

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**Question 10 continued**

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**(Total for Question 10 is 18 marks)**

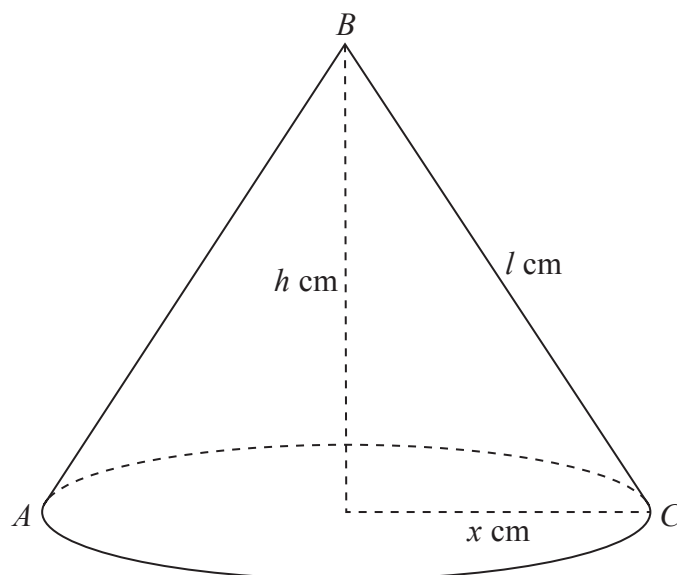


Diagram **NOT**  
accurately drawn

**Figure 2**

Figure 2 shows a right circular cone with a base radius of  $x$  cm. The slant height of the cone is  $l$  cm and the height of the cone is  $h$  cm. The vertex of the cone is  $B$  and the points  $A$  and  $C$ , on the base of the cone, are such that  $AC$  is a diameter of the base.

The cone is increasing in size in such a way that the size of the angle  $ABC$  is constant at  $60^\circ$  and the **total** surface area of the cone is increasing at a constant rate of  $10 \text{ cm}^2/\text{s}$ .

Find the exact rate of increase of the volume of the cone when  $x = 6$

(11)

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**Question 11 continued**

Dotted lines for writing.

**Question 11 continued**

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**Question 11 continued**

Area for writing answers to Question 11, consisting of multiple horizontal dotted lines.

**(Total for Question 11 is 11 marks)**

**TOTAL FOR PAPER IS 100 MARKS**

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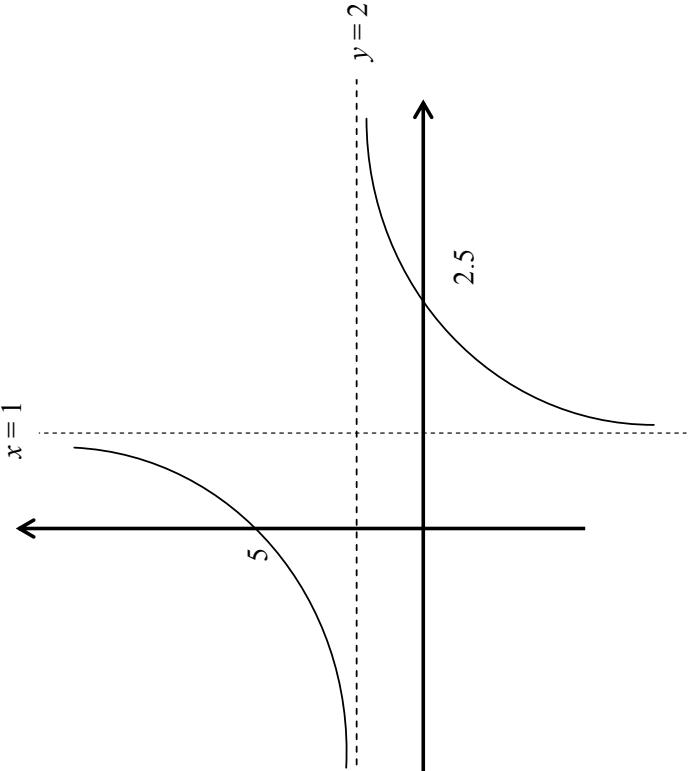
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**International GCSE Further Pure Mathematics – Paper 2 mark scheme**

<b>Paper 2</b>					
<b>Question</b>	<b>Working</b>	<b>Answer</b>	<b>Mark</b>	<b>AO</b>	<b>Notes</b>
<b>1</b>	<p>First term = <math>3e^{-1}</math>, Common Ratio = <math>e^{-2}</math></p> $S = \frac{3e^{-1}}{1 - e^{-2}} \times \left( \frac{e^2}{e^2} \right) = \frac{3e}{e^2 - 1}$ <p>(So, <math>a = 3</math> and <math>b = 2</math>)</p>	$S_{\infty} = \frac{3e}{e^2 - 1}$	<p>B1B1</p> <p>M1M1 A1</p> <p><b>(5)</b></p>	<p>1</p> <p>2</p>	
<b>2</b>					
<b>(a)</b>	$3 + x < 2x - 1 \Rightarrow x > 4$	$x > 4$	B1	1	
<b>(b)</b>	$x(x-1) > 6 \Rightarrow x^2 - x - 6 > 0 \Rightarrow (x-3)(x+2) > 0$ critical values are $x = 3, -2$ so $x > 3$ OR $x < -2$	$x > 3$ OR $x < -2$	M1 M1A1	1	(Outside region)
<b>(c)</b>	$x > 3$ OR $x < -2$ , $x > 4$ so $x > 4$	$x > 4$	B1 <b>(5)</b>	1	

Question	Working	Answer	Mark	AO	Notes
<b>3</b> <b>(a)</b>	$\overline{AB} = -(4i+3j) + (8i+6j) = 4i + (p-3)j$ $ \overline{AB}  = \sqrt{52} = \sqrt{4^2 + (p-3)^2} \Rightarrow p^2 - 6p - 27 = (p-9)(p+3) = 0$ $\Rightarrow p = 9, p = -3$ $(p > 0 \text{ so } p = 9)$		B1 M1A1	1	
<b>(b)</b>	$\overline{AB} = 4i + (p-3)j = 4i + 6j \Rightarrow \frac{1}{2\sqrt{13}}(4i+6j) = \frac{1}{\sqrt{13}}(2i+3j) \text{ (oe)}$	$\frac{1}{2\sqrt{13}}(4i+6j)$	B1B1 <b>(5)</b>	1	
<b>4</b> <b>(a)</b>	$f(-3) = 2 \times (-3)^2 + p \times (-3) + q \times (-3) + 12 = 0$ $\Rightarrow 42 = 9p - 3q \Rightarrow 14 = 3p - q$ $f'(x) = 6x^2 + 2px + q$ $f'(-3) = 6 \times (-3)^2 + 2p \times (-3) + q = 37$ $\Rightarrow -6p + q = -17 \Rightarrow q = 17 - 6p$ $14 = 3p - 1(17 - 6p) \Rightarrow p = 1, q = -11$		M1 M1 M1A1	3	Mark parts (i) and (ii) together
<b>(b)</b>	$\frac{(2x^3 + x^2 - 11x + 12)}{(x+3)} = 2x^2 - 5x + 4$ $\Rightarrow (x+3)(2x^2 - 5x + 4)$	$q = -11$	M1A1  M1A1	2	Solving simultaneous equations (by any method)
<b>(c)</b>	$b^2 - 4ac = (-5)^2 - 4 \times 2 \times 4 = -7 \text{ (7 hence no real roots for quadratic factor, so } x = -3 \text{ only real root.)}$		M1A1 <b>(10)</b>	1	

Question	Working	Answer	Mark	AO	Notes
<b>5</b>					
<b>(a)</b>	$\cos(A-B) - \cos(A+B) = \cos A \cos B + \sin A \sin B - \cos A \cos B + \sin A \sin B$ $\Rightarrow 2 \sin A \cos B$		M1A1	1	
<b>(b)</b>	$2 \sin 5x \sin 3x = \cos 2x - \cos 8x$	$\cos 2x - \cos 8x$	B1	2	
<b>(c)(i)</b>	$\int 4 \sin 5\theta \sin 3\theta d\theta = 2 \int \cos 2\theta - \cos 8\theta d\theta = 2 \left[ \frac{\sin 2\theta}{2} - \frac{\sin 8\theta}{8} \right] (+c)$		M1A1	3	
<b>(ii)</b>	$\int_0^{\frac{\pi}{6}} 4 \sin 5\theta \sin 3\theta dx = 2 \int_0^{\frac{\pi}{6}} (\cos 2\theta - \cos 8\theta) d\theta = 2 \left[ \frac{\sin 2\theta}{2} - \frac{\sin 8\theta}{8} \right]_0^{\frac{\pi}{6}} = \frac{5\sqrt{3}}{8}$	$\frac{5\sqrt{3}}{8}$	M1A1 (7)		
<b>6</b>	$\log_x 2 = \frac{\log_2 2}{\log_2 x} = \frac{1}{\log_2 x}$ $\log_2 x + \frac{6}{\log_2 x} = 7 \Rightarrow (\log_2 x)^2 - 7 \log_2 x + 6 = 0$ $\Rightarrow (\log_2 x - 6)(\log_2 x - 1) = 0 \Rightarrow \log_2 x = 6, \log_2 x = 1$ $\Rightarrow x = 64, x = 2$	64, 2	B1 M1M1 A1 M1M1 A1 (7)	2, 3	

Question	Working	Answer	Mark	AO	Notes
7			M1A1	2	
(a)	$(i) 0 = \frac{ax-5}{x-b} \Rightarrow ax-5=0 \Rightarrow a\frac{5}{2}-5=0 \Rightarrow a=2$	$b=1$	B1	2	Accept $y=5$
(b)	$\text{When } x=0, y = \frac{-5}{-b} \Rightarrow y = \frac{5}{1} \Rightarrow y=5$	$(0, 5)$	B1	3	
(c)	$y=2$	$y=2$	B1	3	
(d)			B1		Curve in correct quadrants
			B1 B1 (8)		Correct asymptotes drawn Correct intersections with axes

Question	Working	Answer	Mark	AO	Notes
8 (a)	$\frac{3}{\sqrt{1-2x}} = 3(1-2x)^{-\frac{1}{2}} \Rightarrow$ $= 3 \left\{ 1 + \left(-\frac{1}{2}\right)(-2x) + \left(-\frac{1}{2}\right)\left(\frac{3}{2}\right)\frac{(-2x)^2}{2!} + \left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(\frac{5}{2}\right)\frac{(-2x)^3}{3!} \dots \right\}$ $\frac{3}{\sqrt{1-2x}} = 3 + 3x + \frac{9}{2}x^2 + \frac{15}{2}x^3$		B1	2	
(b)	$-\frac{1}{2} < x < \frac{1}{2} \text{ or }  x  < \frac{1}{2}$	$-\frac{1}{2} < x < \frac{1}{2}$	B1	2	
(c)	$\frac{3}{\sqrt{0.9}} = \frac{3}{\sqrt{\frac{9}{10}}} = \frac{3}{\frac{3}{\sqrt{10}}} = \sqrt{10}$		B1	3	
(d)	$\frac{1}{\sqrt{10}-3} \times \frac{(\sqrt{10}+3)}{(\sqrt{10}+3)} = \frac{(\sqrt{10}+3)}{1} = (\sqrt{10}+3)$	$(\sqrt{10}+3)$	M1A1	3	
(e)	$1-2x=0.9 \Rightarrow x=0.05$ $\sqrt{10}+3 = 3 + 3 \times (0.05) + \frac{9}{2} \times (0.05)^2 + \frac{15}{2} \times (0.05)^3 + \dots + 3 = 3.1621875 \dots + 3$ $\approx 6.16219$	$6.16219$	B1 M1A1 (11)	3	

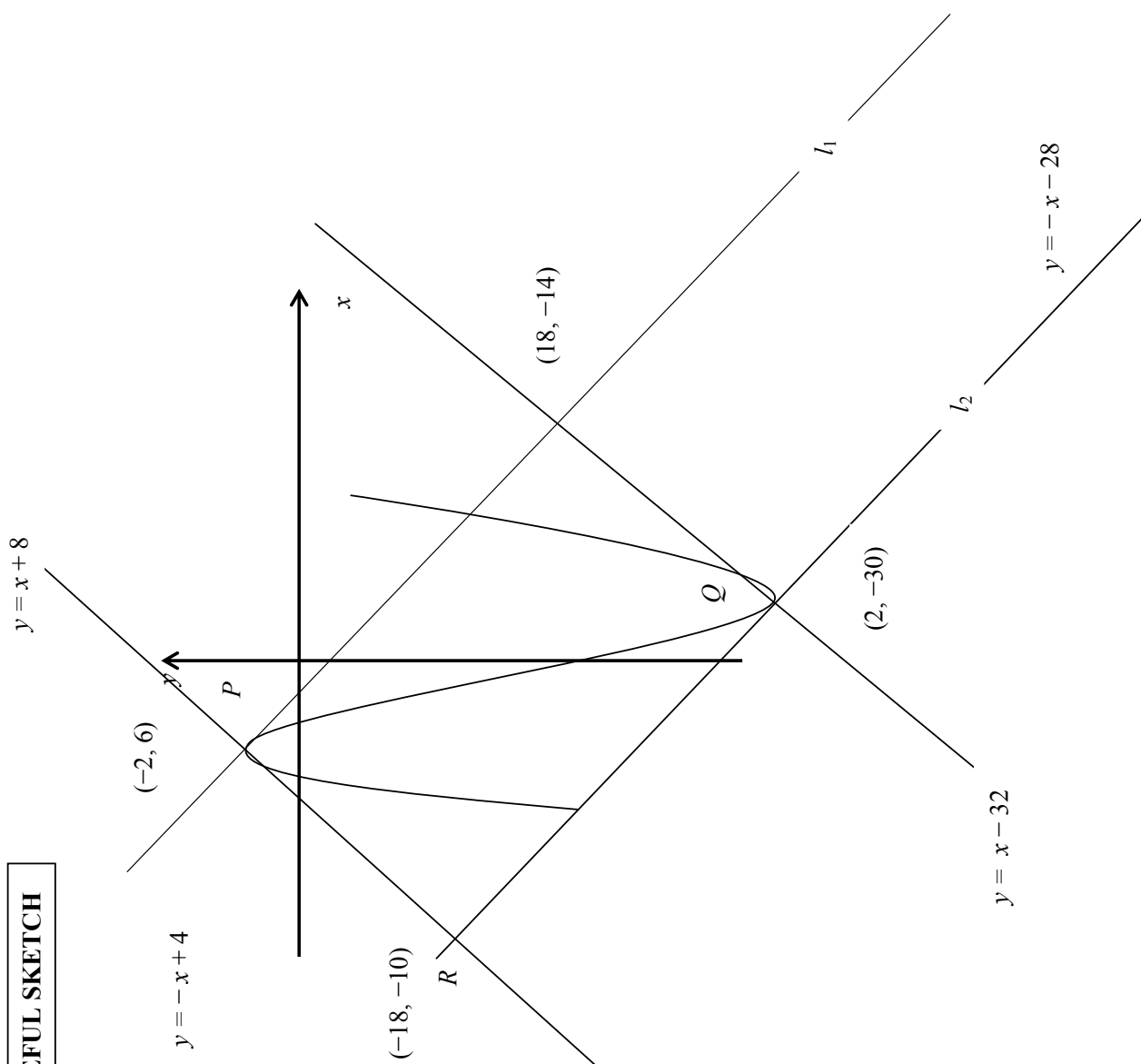
Question	Working	Answer	Mark	AO	Notes
<b>9</b> <b>(a)</b>	$7 + 4x - 2x^2 = -2[(x-1)^2 - 1] + 7 = -2(x-1)^2 + 9$ $P = -2, Q = -1, R = 9$		M1A1 A1	1	
<b>(b)</b>	(i) 9 (ii) 1	(i) 9 (ii) 1	B1B1	2	
<b>(c)</b>	$7 + 4x - 2x^2 = 4 - x \Rightarrow 2x^2 - 5x - 3 = 0$ $\Rightarrow (2x+1)(x-3) = 0 \Rightarrow x = -\frac{1}{2}, 3$	$x = -\frac{1}{2}, x = 3$	M1M1 A1	2	
<b>(d)</b>	$V = \pi \int_{-0.5}^3 (7 + 4x - 2x^2)^2 dx = \pi \int_{-0.5}^3 (4-x)^2 dx$ $\Rightarrow \pi \int_{-0.5}^3 33 + 64x - 13x^2 - 16x^3 + 4x^4 dx$ $\Rightarrow \pi \left[ 33x + 32x^2 - \frac{13x^3}{3} - 4x^4 + \frac{4x^5}{5} \right]_{-0.5}^3 = \pi \frac{4459}{30} = 466.945... \approx 467$	467	M1  M1A1 M1A1 <b>(13)</b>	3	





Question	Working	Answer	Mark	AO	Notes
10 cont'd (d)	<p>{Coordinates of <math>R</math> <math>(-18, -10)</math>}</p> $PR = \sqrt{(6 - -10)^2 + (-2 - -18)^2} = 16\sqrt{2}$	$16\sqrt{2}$	M1A1	3	
(e)	<p>Area of rectangle</p> <p>Length of <math>QR = \sqrt{(-18 - 2)^2 + (-10 - -30)^2} = 20\sqrt{2}</math></p> <p>Area = <math>16\sqrt{2} \times 20\sqrt{2} = 640</math></p>	640	M1 M1A1	3	
(e)	<p><b>ALTERNATIVE</b></p> <p>Equation of normal at <math>Q</math></p> $y - -30 = x - 2 \Rightarrow y = x - 32$ <p>Coordinates of 4<sup>th</sup> vertex of rectangle</p> $x - 32 = -x + 4 \Rightarrow x = 18 \text{ so } y = -14$ $\text{Area} = \frac{1}{2} \begin{vmatrix} -2 & -18 & 2 & 18 \\ 6 & -10 & -30 & -14 \\ -14 & 6 & 6 & 6 \end{vmatrix} = 640$	640	M1 M1A1 (18)	3	

**USEFUL SKETCH**



Question	Working	Answer	Mark	AO	Notes
11	<p>Total Surface Area of the cone</p> $l = \frac{x}{\sin 30^\circ} = 2x$ $A = \pi r l + \pi r^2 \Rightarrow \pi x \times 2x + \pi x^2 = 3\pi x^2$ <p>Volume of cone</p> $h = \frac{x}{\tan 30^\circ} = \sqrt{3}x$ $\text{Vol} = \frac{1}{3} \pi r^2 h \Rightarrow V = \frac{\sqrt{3}}{3} \pi x^3$ $\frac{dA}{dt} = 10 \text{ (cm}^2 \text{ / s)} \quad \frac{dV}{dx} = \sqrt{3} \pi x^2, \frac{dA}{dx} = 6\pi x$ $\frac{dV}{dt} = \frac{dV}{dx} \times \frac{dx}{dt} \times \frac{dA}{dx}$ $\Rightarrow \frac{dV}{dt} = \sqrt{3} \pi x^2 \times 10 \times \frac{1}{6\pi x} = \frac{5\sqrt{3}}{3} x \Rightarrow 10\sqrt{3} \text{ (cm}^3 \text{ / s)}$	$10\sqrt{3} \text{ (cm}^3 \text{ / s)}$	<p>B1</p> <p>M1A1</p> <p>B1</p> <p>M1A1</p> <p>B1M1</p> <p>M1</p> <p>M1A1</p> <p>(11)</p> <p>100</p>	2, 3	M1 for differentiating $\frac{dV}{dx}$ or $\frac{dA}{dx}$ <b>either</b>
		<b>Total</b>	<b>100</b>		



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